

Assignment #2 Definite Integral

This assignment should be completed and sent to me on or before May 4/20.

All answers should be neat and clear.

Question 1 a,c,e,g,i,k,n,o

Question 3 a,b,c

The answers are given so it is the procedure I am looking for.

noticed by Isaac Barrow, was used by Newton and Leibniz to develop calculus a powerful method for solving problems in mathematical science.

1. Evaluate the following definite integrals.

(a) $\int_{-6}^7 2 \, dx$

(b) $\int_{-1}^5 (6x - 7) \, dx$

(c) $\int_1^2 (5 + 4x - 6x^2) \, dx$

(d) $\int_0^1 (t^2 + 6t - 1) \, dt$

(e) $\int_{-1}^2 (x^3 - x^2 + 4x) \, dx$

(f) $\int_0^1 (x^{99} + 1) \, dx$

(g) $\int_2^3 \frac{1}{t^2} \, dt$

(h) $\int_1^4 (x - \sqrt{x}) \, dx$

(i) $\int_0^1 \sqrt[4]{x^5} \, dx$

(j) $\int_1^8 \frac{2}{\sqrt[3]{x}} \, dx$

(k) $\int_1^2 \frac{x^3 + x^2 + 1}{x^3} \, dx$

(l) $\int_1^4 \left(\frac{\sqrt{x} + 1}{x} \right) \, dx$

(m) $\int_0^{64} \sqrt{y}(1 + \sqrt[3]{y}) \, dy$

(n) $\int_0^{\frac{\pi}{2}} (8x + \cos x) \, dx$

(o) $\int_0^{\frac{\pi}{6}} (\sec x \tan x) \, dx$

(p) $\int_{\frac{\pi}{4}}^{\frac{\pi}{3}} (3 \sin \theta - \sec^2 \theta) \, d\theta$

3. Evaluate each integral.

(a) $\int_0^1 e^x dx$

(b) $\int_{-1}^1 2^x dx$

(c) $\int_0^{\frac{1}{2}} \frac{1}{\sqrt{1-x^2}} dx$

(d) $\int_1^{\sqrt{3}} \frac{12}{1+x^2} dx$

(e) $\int_{-1}^1 \left(x + 1 + \frac{3}{x^2 + 1} \right) dx$

(f) $\int_{-\pi}^0 (2e^x + \sin x) dx$

4. What is wrong with the following calculation?

$$\int_{-2}^1 \frac{1}{x^4} dx = \frac{x^{-3}}{-3} \Big|_{-2}^1 = -\frac{1}{3x^3} \Big|_{-2}^1 = -\frac{1}{3} - \frac{1}{24} = -\frac{1}{8}$$

PROBLEMS PLUS

Given that the area above the x -axis is equal to the area below the x -axis, find the equation of the parabola.



EXERCISE 11.2

1. (a) 26 (b) 30 (c) -3 (d) $\frac{7}{3}$ (e) $\frac{27}{4}$ (f) 1.01

(g) $\frac{1}{6}$ (h) $\frac{17}{6}$ (i) $\frac{4}{9}$ (j) 9 (k) $\frac{11}{8} + \ln 2$

(l) $2 + \ln 4$ (m) $\frac{48 \ 128}{33}$ (n) $\pi^2 + 1$

(o) $\frac{2}{\sqrt{3}} - 1$ (p) $\frac{1}{2}(3\sqrt{2} - 1) - \sqrt{3}$

2. (a) $\frac{1}{6}x^6 - \frac{1}{2}x^4 + 4x + C$ (b) $\frac{2}{7}x^{\frac{7}{2}} + C$

(c) $\frac{1}{2}t^2 + 2 \ln|t| + C$

(d) $x + \frac{4}{3}x^{\frac{3}{2}} + \frac{1}{2}x^2 + C$ (e) $\frac{4}{7}x^{\frac{7}{4}} - \frac{20}{3}x^{\frac{3}{4}} + C$

(f) $\sin \theta - \cos \theta + C$ (g) $x^5 + 2 \csc x + C$

(h) $x - 2 \cot x + C$

3. (a) $e - 1$ (b) $\frac{3}{2 \ln 2}$ (c) $\frac{\pi}{6}$ (d) π

(e) $2 + \frac{3}{2}\pi$ (f) $-2e^{-\pi}$

4. The function is not continuous on $[-2, 1]$, so