

Section 6.4 Page 349 Question 14

a)

	Distance (km)	Rate (km/h)	Time (h)
Downstream	18	$x + 3$	$\frac{18}{x+3}$
Upstream	8	$x - 3$	$\frac{8}{x-3}$

b)
$$\frac{18}{x+3} = \frac{8}{x-3}$$

c)
$$\frac{18}{x+3} = \frac{8}{x-3}$$

$$18(x-3) = 8(x+3)$$

$$18x - 54 = 8x + 24$$

$$10x = 78$$

$$x = 7.8$$

The rate of the kayakers in still water is 7.8 km/h.

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	Distance (km)	Speed (km/h)	Time (h)
To Forde Lake	70	$x - 5$	$\frac{70}{x - 5}$
Beyond Forde Lake	60	x	$\frac{60}{x}$

$$\frac{70}{x - 5} - 4(24) = \frac{60}{x}$$

$$70x - 96x(x - 5) = 60(x - 5)$$

$$70x - 96x^2 + 480x = 60x - 300$$

$$0 = 96x^2 - 490x - 300$$

$$0 = 48x^2 - 245x - 150$$

$$x = \frac{-(-245) \pm \sqrt{(-245)^2 - 4(48)(-150)}}{2(48)}$$

$$x = \frac{245 \pm \sqrt{88\,825}}{96}$$

$$x = 5.6566\dots$$

The average speed of the herd beyond Forde Lake was 5.7 km/h, to the nearest tenth of a kilometre per hour.

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Let x kilometres per hour represent Ted's speed east of Swift Current.

	Distance (km)	Speed (km/h)	Time (h)
West of Swift Current	275	$x - 10$	$\frac{275}{x-10}$
East of Swift Current	300	x	$\frac{300}{x}$

$$\frac{275}{x-10} = \frac{300}{x} + \frac{1}{2}$$

$$2(x)275 = 300(2)(x-10) + x(x-10)$$

$$550x = 600x - 6000 + x^2 - 10x$$

$$0 = x^2 + 40x - 6000$$

$$0 = (x+100)(x-60)$$

$$x = -100 \text{ or } x = 60$$

Ted's average speed east of Swift Current was 60 km/h and west of Swift Current it was 50 km/h.

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Let x kilometres per hour represent the speed of the current.

	Distance (km)	Speed (km/h)	Time (h)
Up river	2	$6 - x$	$\frac{2}{6-x}$
Down river	2	$6 + x$	$\frac{2}{6+x}$

Use the fact that the total time to paddle up river and back is 1 h to write an equation.

$$\frac{2}{6-x} + \frac{2}{6+x} = 1$$

$$2(6+x) + 2(6-x) = (6+x)(6-x)$$

$$12 + 2x + 12 - 2x = 36 - x^2$$

$$x^2 = 12$$

$$x = \sqrt{12}$$

$$x \approx 3.5$$

The speed of the current is approximately 3.5 km/h.